	CS483-07 Divide and Conquer
	Instructor: Fei Li
	Room 443 ST II
Offi	ice hours: Tue. & Thur. 1:30pm - 2:30pm or by appointments
	lifei@cs.gmu.edu with subject: CS483
http://	'www.cs.gmu.edu/ $\sim$ lifei/teaching/cs483_fall07/
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Problem size: *n*. Divide the problems into *b* smaller instances; *a* of them need to be solved. f(n) is the time spent on dividing and merging.

$$T(n) = aT(n/b) + f(n)$$

▶ Master Theorem: If  $f(n) \in \Theta(n^d)$ , where  $d \ge 0$ , then

$$T(n) = \begin{cases} \Theta(n^d) & \text{if } a < b^d \\ \Theta(n^d \log n) & \text{if } a = b^d \\ \Theta(n^{\log_b a}) & \text{if } a > b^d \end{cases}$$

3

CS483 Design and Analysis of Algorithms



Lecture 07, September 18, 2007









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	Imagine that you are placed in an unknown building and you are given a room
	number (say STII, 443), you need to find your CS 483 instructor. What will
	Binary Search:
	Very efficient algorithm for searching in <b>sorted array</b> Event algorithm for searching in <b>sorted array</b>
	<b>Example</b> : find 70 in {3, 14, 27, 31, 39, 42, 55, 70, 74, 81, 85, 93, 98}
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483 De	sign and Analysis of Algorithms 13 Lecture 07, September 18, 24
183 De	sign and Analysis of Algorithms 13 Lecture 07, September 18, 24 Binary Search - Algorithm
183 De	sign and Analysis of Algorithms 13 Lecture 07, September 18, 24 Binary Search - Algorithm Given a sorted array A of n numbers, find a key K in A
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483 De	sign and Analysis of Algorithms 13 Lecture 07, September 18, 24 Binary Search - Algorithm Given a sorted array $A$ of $n$ numbers, find a key $K$ in $A$
483 De	sign and Analysis of Algorithms       13       Lecture 07, September 18, 20         Binary Search - Algorithm       Sign and Analysis of Algorithm         Given a sorted array $A$ of $n$ numbers, find a key $K$ in $A$











## Summary of Sorting Algorithms

selection-sort	$O(n^2)$	small inputs)
insertion-sort	$O(n^2)$	in-place. slow (good for small inputs)
quick-sort	expected $O(n \log n)$	in-place, randomized, fastest (good for large inputs)
merge-sort	$O(n \log n)$	sequential data access. fast (good for huge inputs)