

Iteration Method: Examples • n! T(n) = T(n-1) + 1• Tower of Hanoi T(n) = 2T(n-1) + 1CS483 Design and Analysis of Algorithms 5 Lecture 05, September 11, 2007 Iteration: Example • n! (T(n) = T(n-1) + 1)T(n) = T(n-1) + 1= (T(n-2)+1)+1= T(n-2) + 2... ... = T(n-i) + i... ... = T(0) + n = n• Tower of Hanoi (T(n) = 2T(n-1) + 1) ???

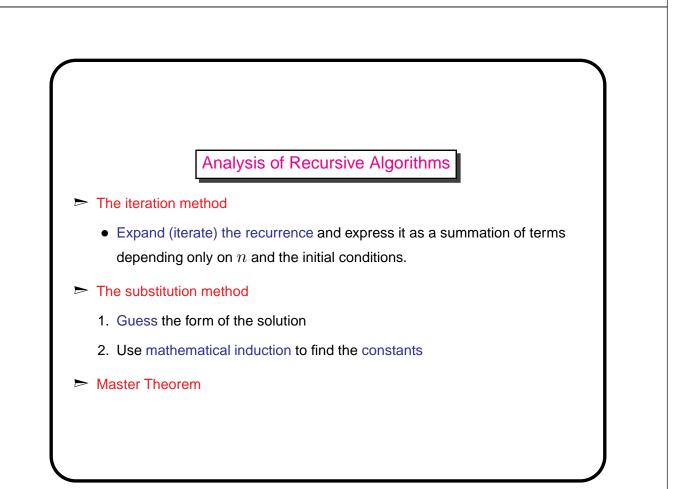
Tower of Hanoi (T(n) = 2T(n-1) + 1)

$$T(n) = 2T(n-1) + 1$$

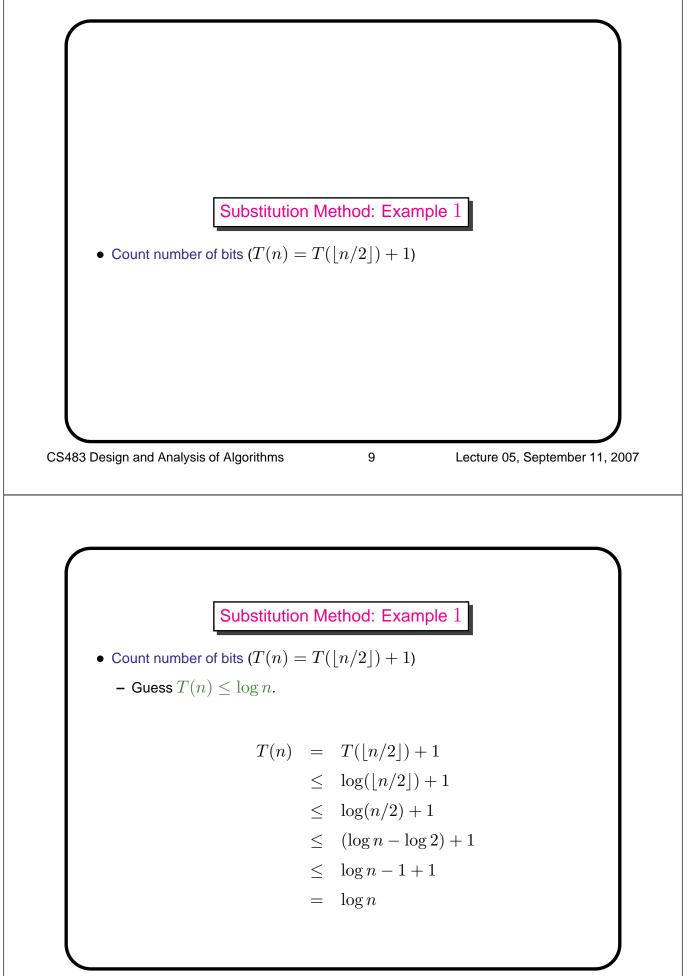
= 2(2T(n-2) + 1) + 1
= 2²T(n-2) + 2 + 1
...
= 2ⁱT(n-i) + 2ⁱ⁻¹ + ... + 1
...
= 2ⁿ⁻¹T(1) + 2ⁿ⁻¹ + 2ⁿ⁻¹ + ... + 1
= 2ⁿ⁻¹T(1) + \sum_{i=0}^{n-2} 2^i
= 2ⁿ⁻¹ + 2ⁿ⁻¹ - 1
= 2ⁿ - 1

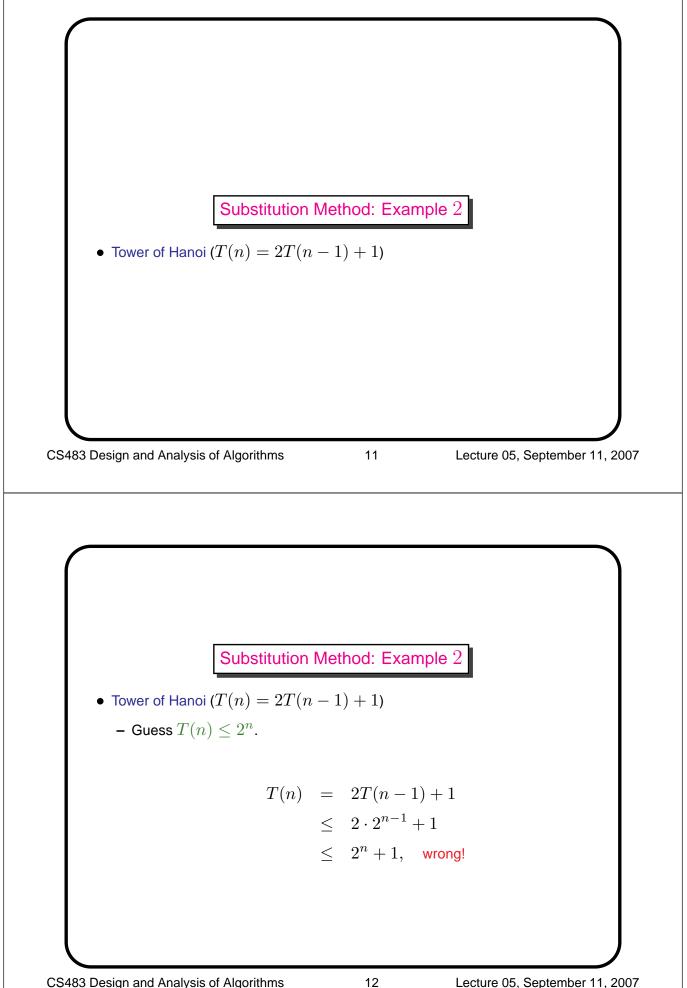
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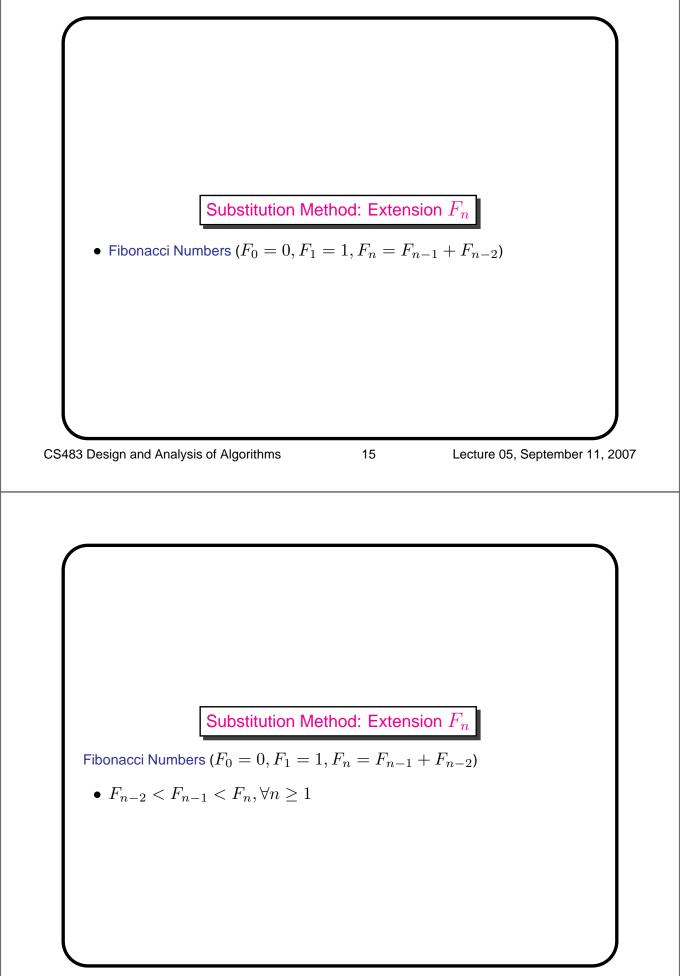


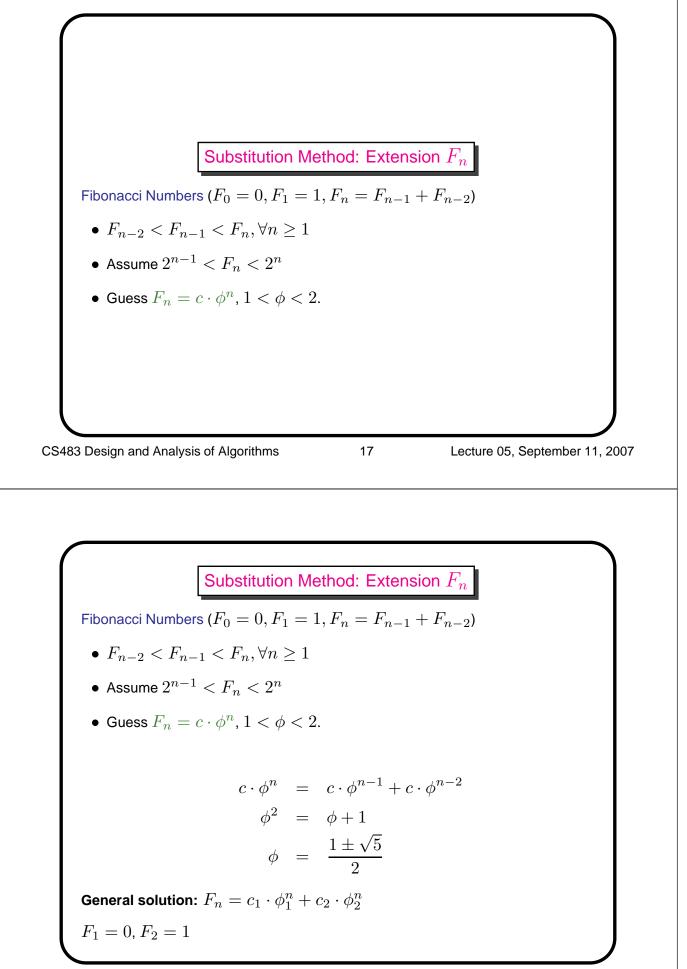
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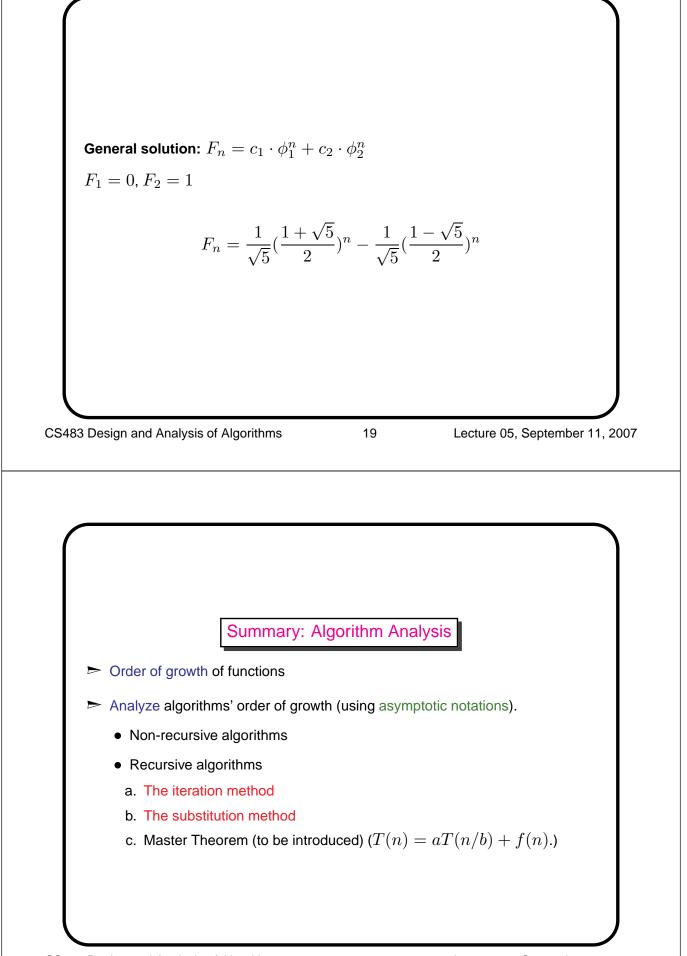




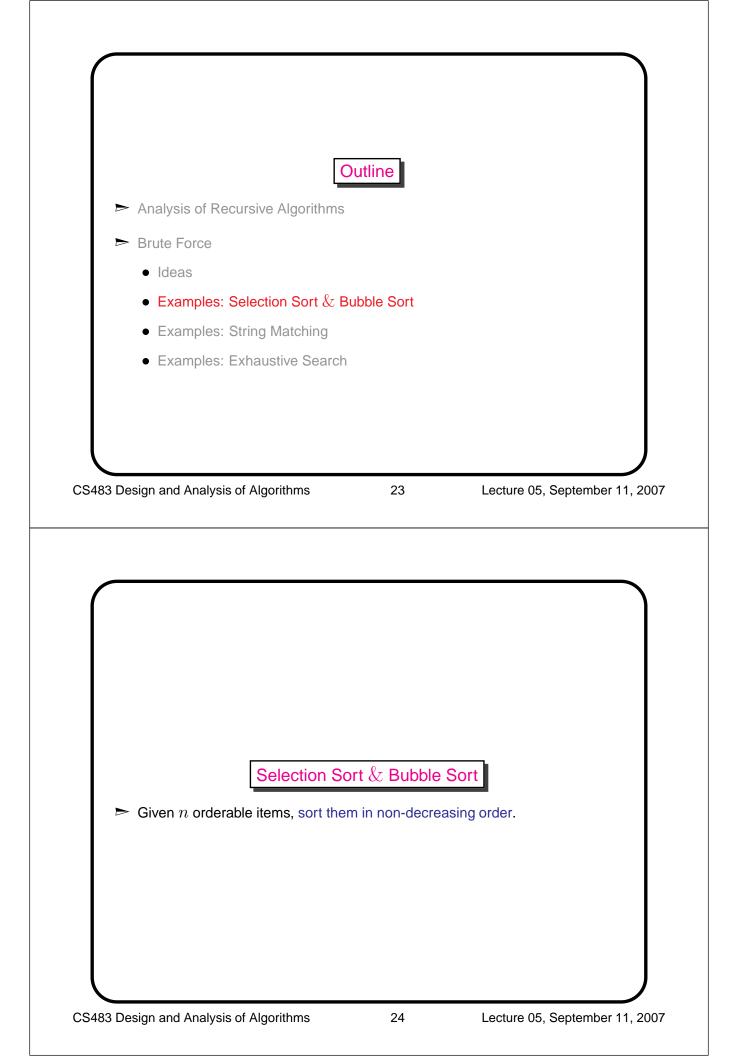
Substitution Method: Extension F_n • Tower of Hanoi (T(n) = 2T(n-1) + 1) – Guess $T(n) \leq 2^n$. T(n) = 2T(n-1) + 1 $\leq 2 \cdot 2^{n-1} + 1$ $\leq 2^n + 1$, wrong! - Guess $T(n) \le 2^n - 1$. CS483 Design and Analysis of Algorithms 13 Lecture 05, September 11, 2007 T(n) = 2T(n-1) + 1 $\leq 2(2^{n-1}-1)+1$ $= 2^n - 2 + 1$ $= 2^n - 1$, correct!

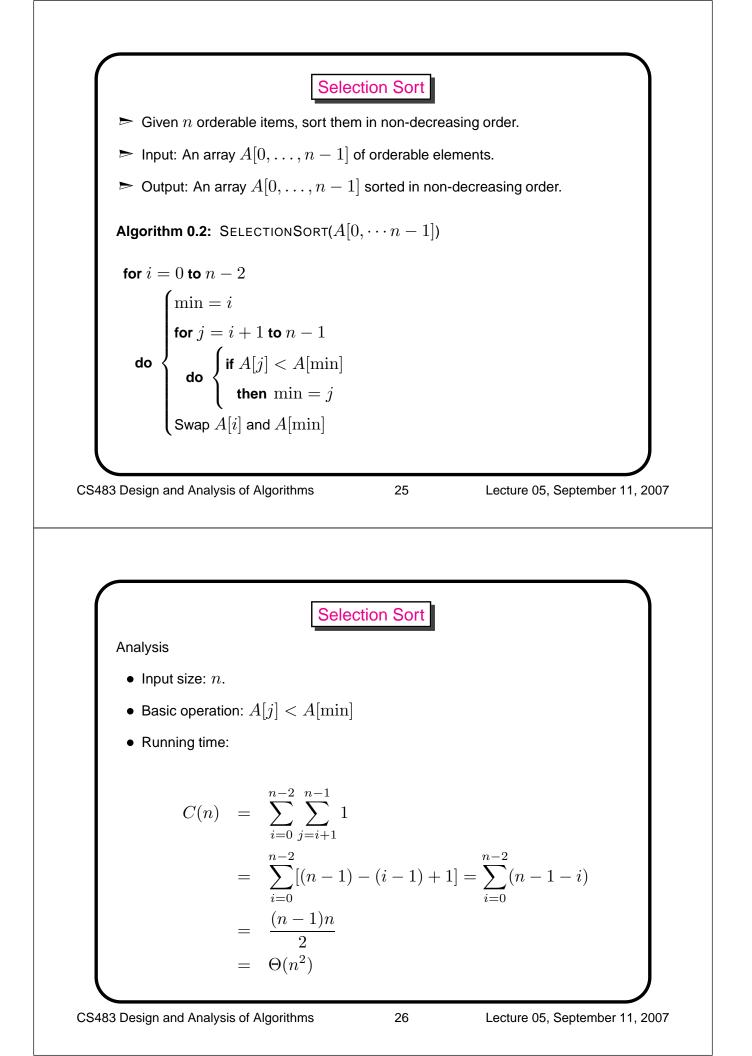


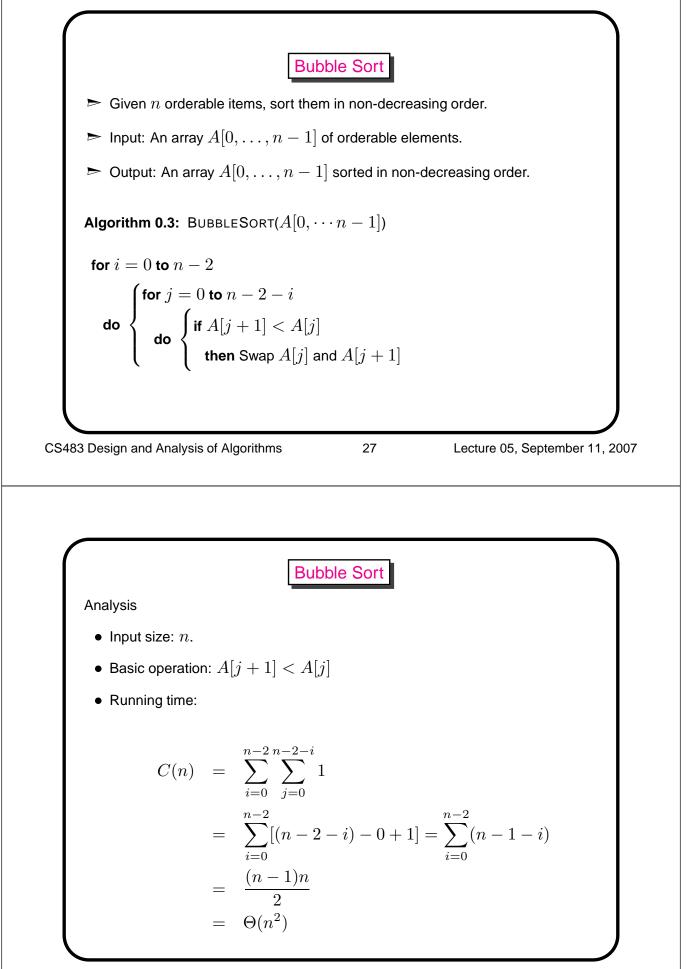


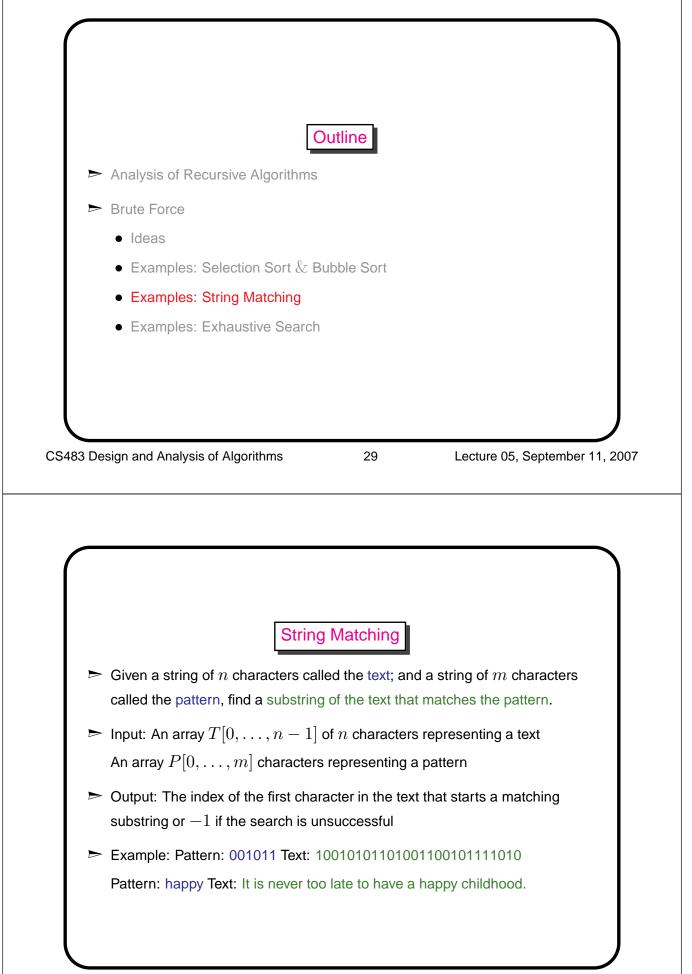


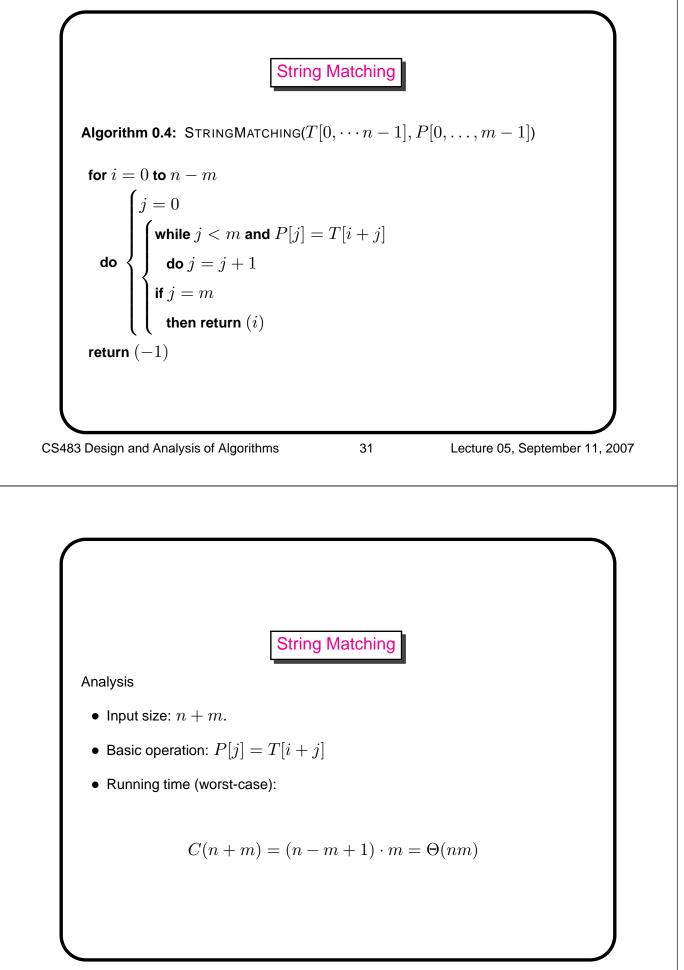
	Outline	
 Analysis of Recursive Algorithm 	IS	
Brute Force		
• Ideas		
• Examples: Selection Sort &	Bubble Sort	
• Examples: String Matching		
Examples: Exhaustive Searce	ch	
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Pruto		a.
-	Force — Ideas	
Brute force is a straightforward	approach to solv	e a problem, usually directly
-	approach to solv	e a problem, usually directly

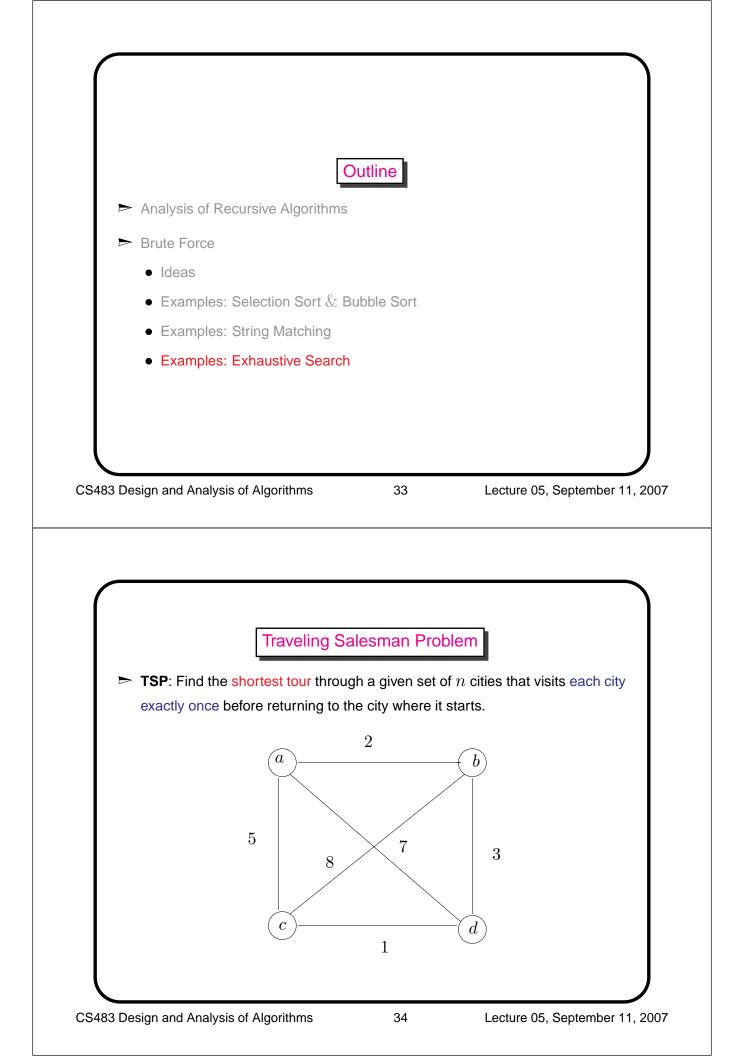


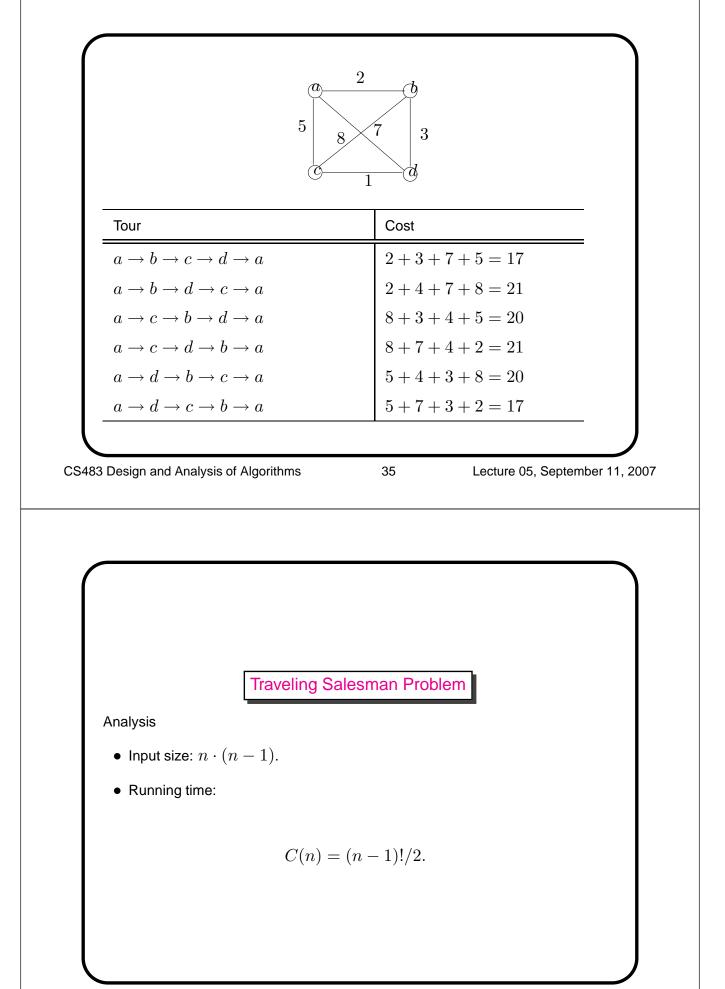


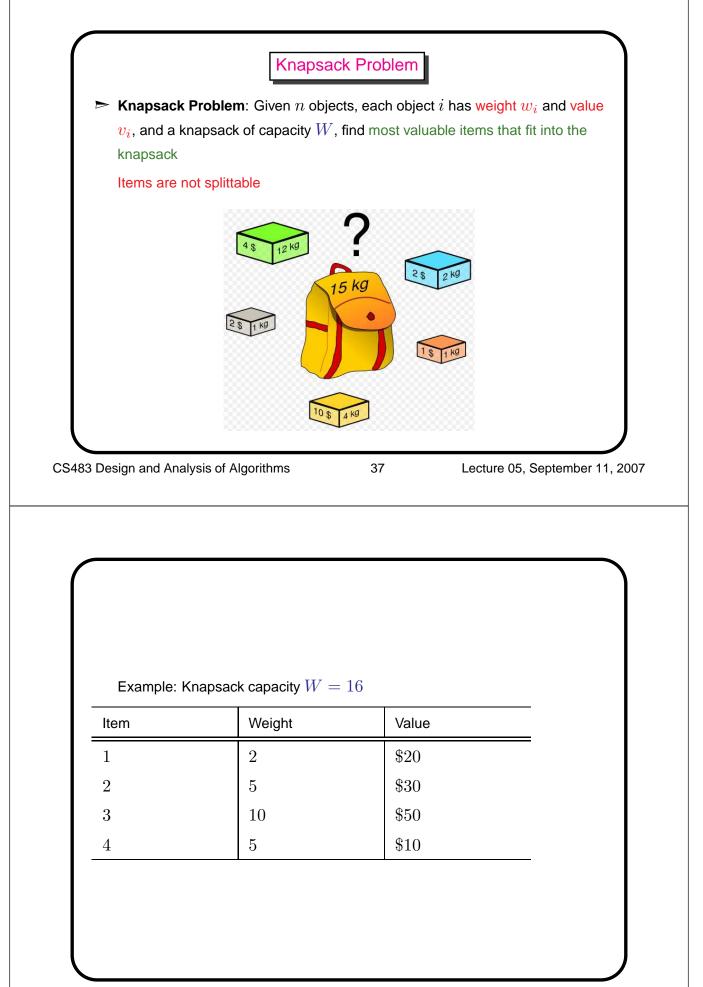












Subset	Total weight	Total value	
{1}	2	\$20	
$\{2\}$	5	\$30	
{3}	10	\$50	
{4}	5	\$10	
$\{1, 2\}$	7	\$50	
$\{1, 3\}$	12	\$70	
$\{1, 4\}$	7	\$30	
$\{2, 3\}$	15	\$80	
$\{2, 4\}$	10	\$40	
$\{3, 4\}$	15	\$60	
$\{1, 2, 3\}$	17	not feasible	
$\{1, 2, 4\}$	12	\$60	
$\{1, 3, 4\}$	17	not feasible	
$\{2, 3, 4\}$	20	not feasible	
$\{1, 2, 3, 4\}$	22	not feasible	
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Design and Analysis	s of Algorithms		eptember 11,
			eptember 11,
	Knapsack		eptember 11,
nalysis	Knapsack		eptember 11,
Running time:	Knapsack	Problem	eptember 11,

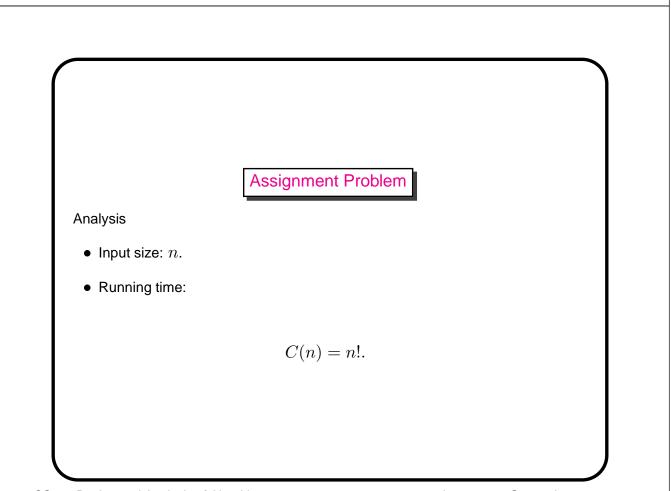
Assignment Problem

Assignment Problem: There are n people to execute n jobs, one person per job. If *i*th person is assigned the *j*th job, the cost is C[i, j], i, j = 1, ..., n. Find the assignment with the minimum total cost.

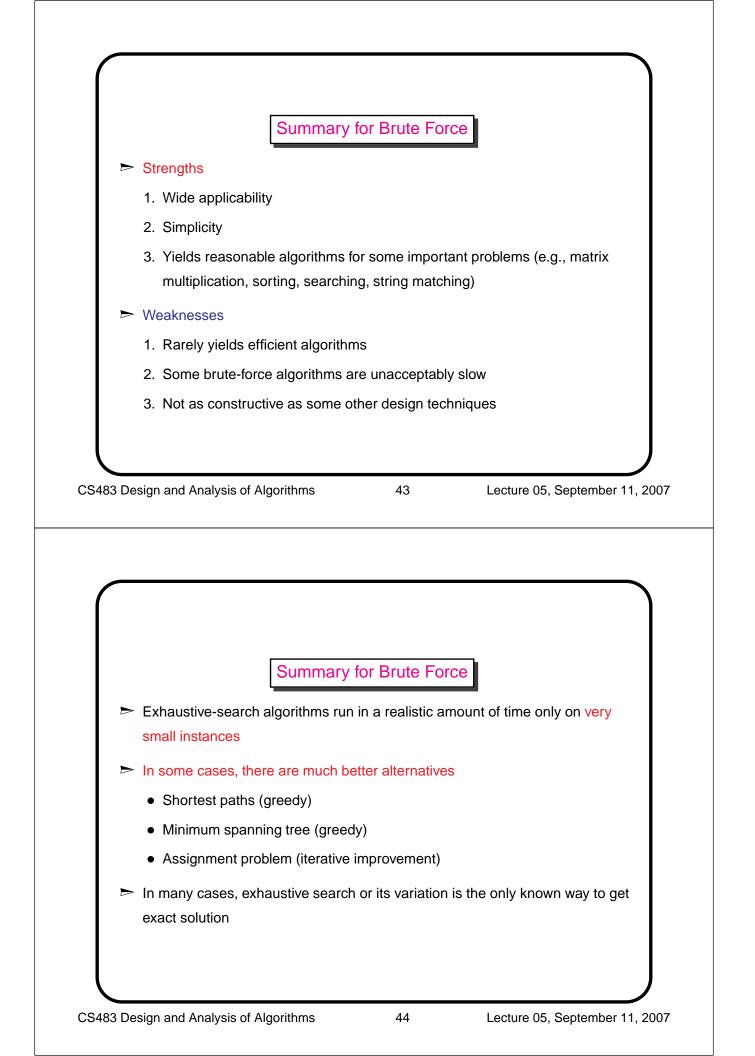
	Job 1	Job 2	Job 3	Job 4
Person 1	9	2	7	8
Person 2	6	4	3	7
Person 3	5	8	1	8
Person 4	7	6	9	4

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		Summary	
► Read Ch	ар. 3.		
Next clas	s: Chap. 4 and Mast	ter Theorem.	