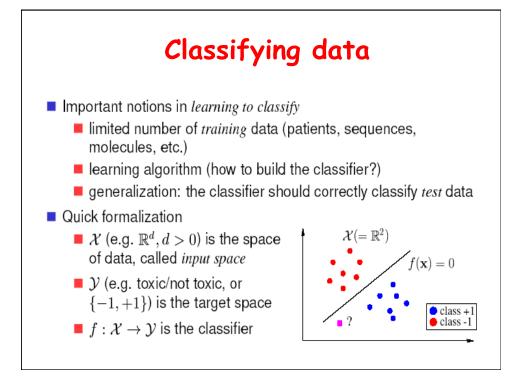
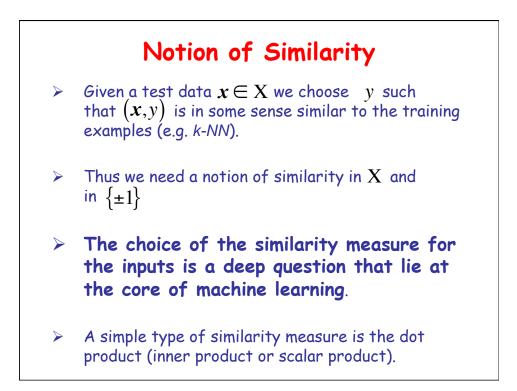
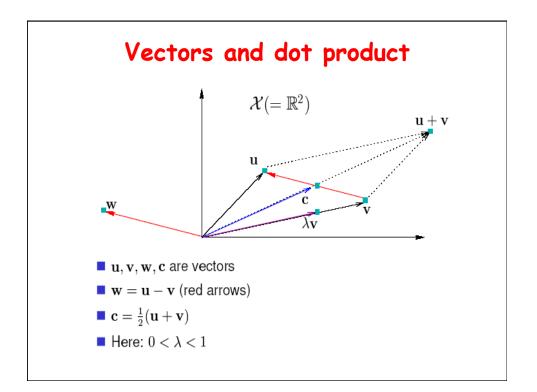
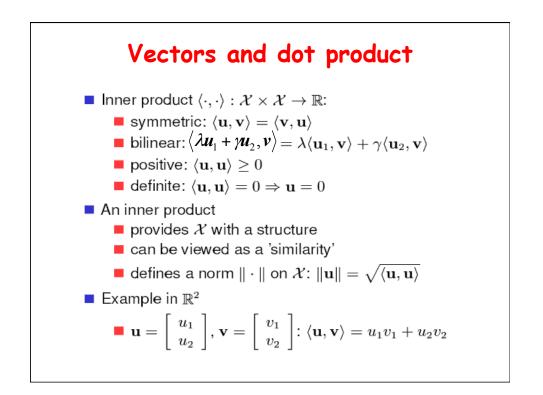
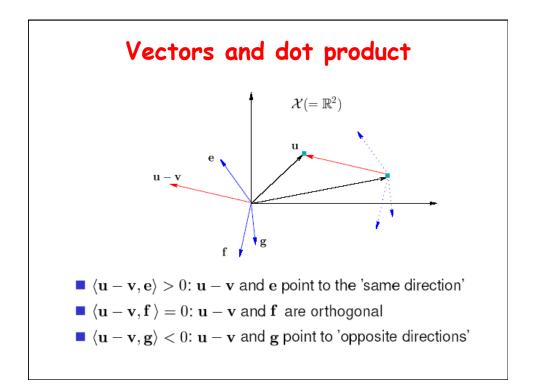
Introduction to Kernel Methods

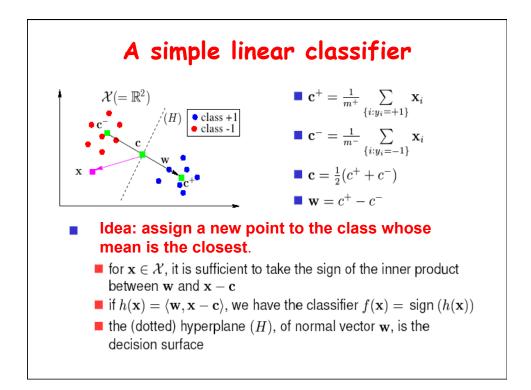


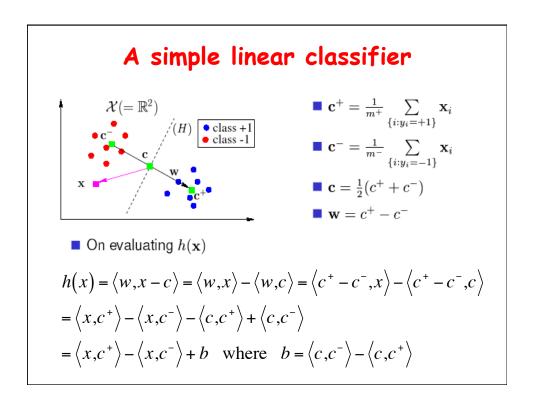












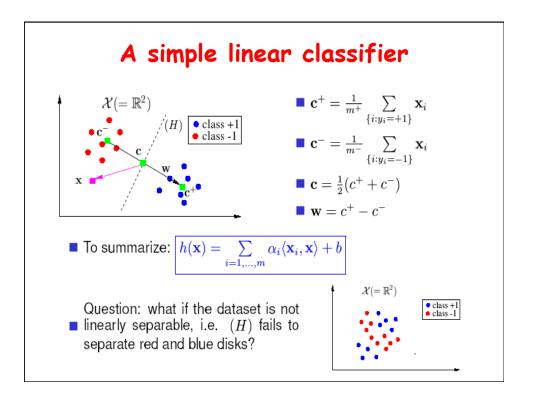
$$A \text{ simple linear classifier}$$

$$h(x) = \langle x, c^+ \rangle - \langle x, c^- \rangle + b$$

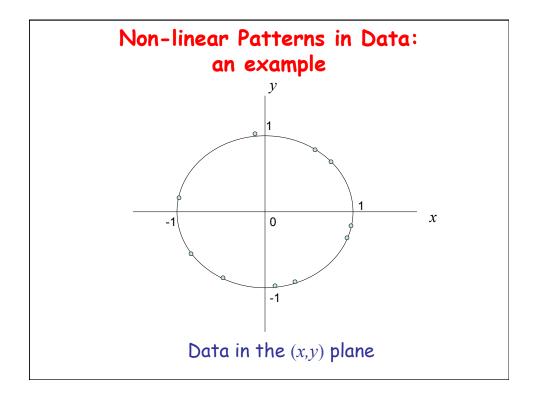
$$= \langle x, \frac{1}{m^+} \sum_{i:y_i=1} x_i \rangle - \langle x, \frac{1}{m^-} \sum_{i:y_i=-1} x_i \rangle + b$$

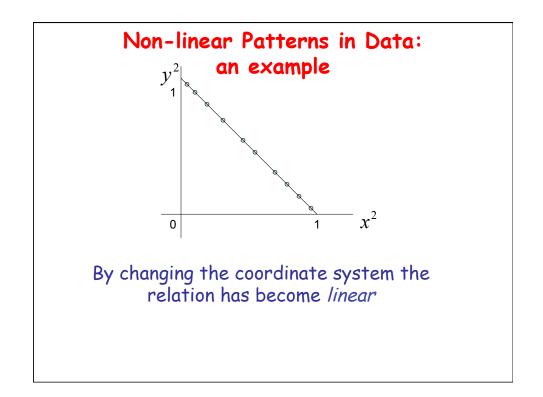
$$= \frac{1}{m^+} \sum_{i:y_i=1} \langle x, x_i \rangle - \frac{1}{m^-} \sum_{i:y_i=-1} \langle x, x_i \rangle + b$$

$$= \sum_{i=1}^m \alpha_i \langle x, x_i \rangle + b$$
where $\alpha_i = \frac{1}{m^+} \forall i: y_i = 1$ and $\alpha_i = \frac{1}{m^-} \forall i: y_i = -1$



Non-linear Patterns in Data: an example				
Х	У	x^2	y^2	xy
0.8415	0.5403	0.7081	0.2919	0.4546
0.9093	-0.4161	0.8268	0.1732	-0.3784
0.1411	-0.99	0.0199	0.9801	-0.1397
-0.7568	-0.6536	0.5728	0.4272	0.4947
-0.9589	0.2837	0.9195	0.0805	-0.272
-0.2794	0.9602	0.0781	0.9219	-0.2683
0.657	0.7539	0.4316	0.5684	0.4953
0.9894	-0.1455	0.9788	0.0212	-0.144
0.4121	-0.9111	0.1698	0.8302	-0.3755
-0.544	-0.8391	0.296	0.704	0.4565



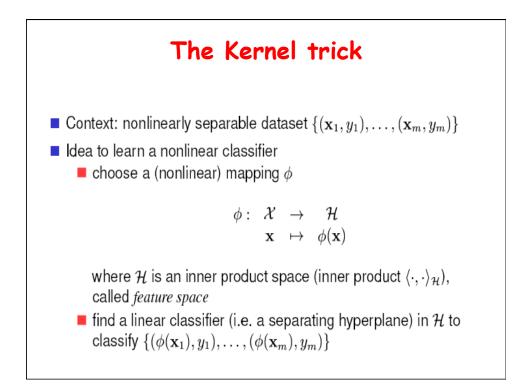


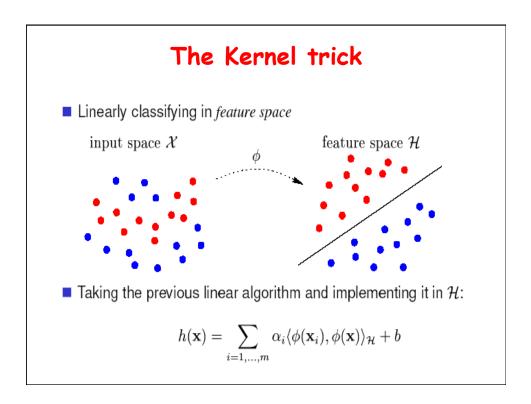
Non-linear Patterns in Data: an example

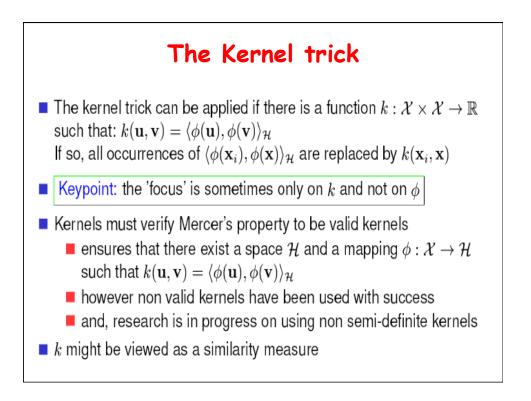
> Using the initial coordinates, the pattern was expressed as a *quadratic* form:

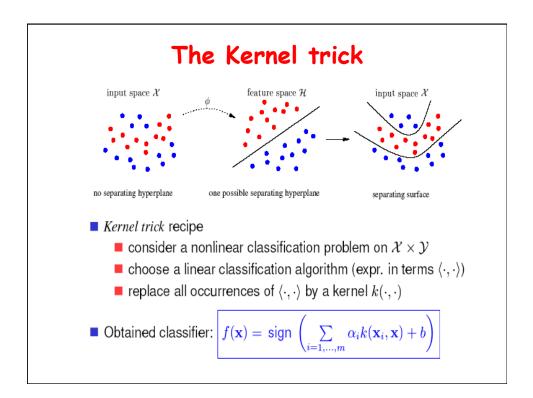
$$f(\mathbf{x}) = x^2 + y^2 - 1 = 0 \qquad \forall \mathbf{x}$$

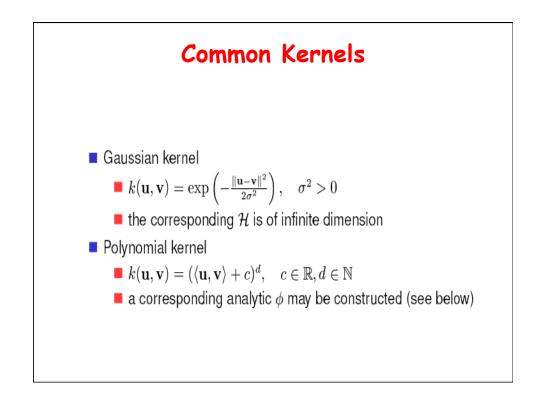
- > In the coordinate system using monomials, it appeared as a *linear* function.
- The possibility of transforming the representation of a pattern by changing the coordinate system in which the data are described is a recurrent theme in kernel methods.

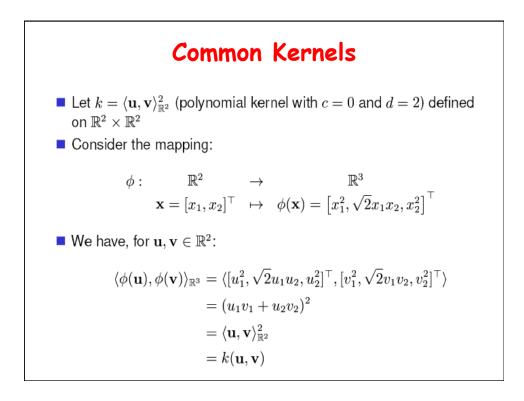


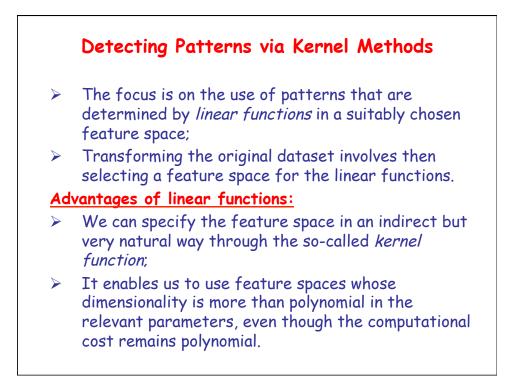


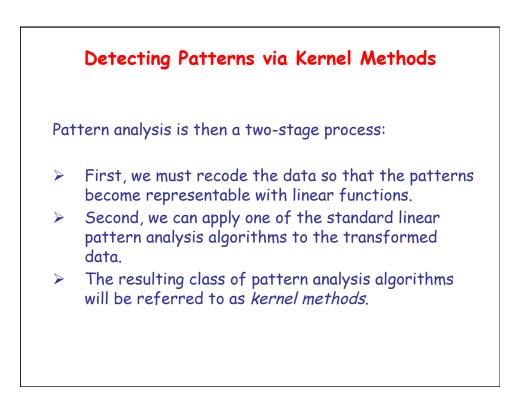


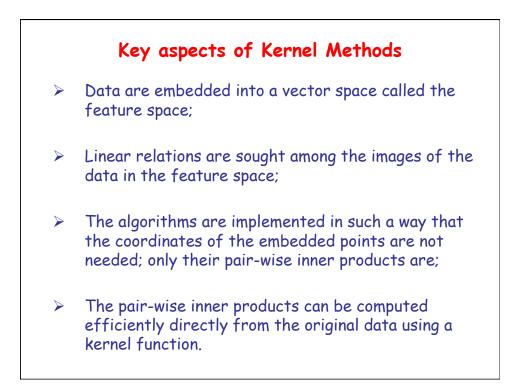


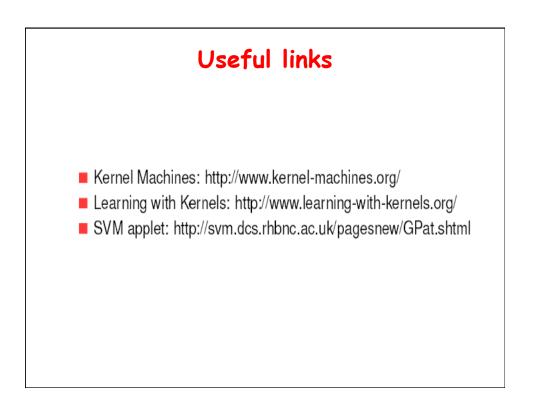












References

- J. Shawe-Taylor and N. Cristianini, Kernel Methods for Pattern Analysis. Pattern analysis (Chapter 1).
- B. Scholkopf and A. Smola, *Learning with Kernels*. A Tutorial Introduction (Chapter 1). MIT University Press.