CS 688 – Fall 2013

Homework 2 – Due October 1

Professor: Carlotta Domeniconi

Problem 1 Solve exercises 4.5 and 4.8 of the textbook.

Problem 2 Show that for $K > 2$ classes, under the assumption of Gaussian class-conditional densities with equal covariance matrices, the posterior probability $p(C_k|\mathbf{x}_n)$ can be written as follows:

$$p(C_k|\mathbf{x}_n) = \frac{e^{\mathbf{w}_k^T\mathbf{x}+w_{k0}}}{\sum_j e^{\mathbf{w}_j^T\mathbf{x}+w_{j0}}}$$

where $\mathbf{w}_k = \Sigma^{-1}\boldsymbol{\mu}_k$ and $w_{k0} = -\frac{1}{2}\boldsymbol{\mu}_k^T\Sigma^{-1}\boldsymbol{\mu}_k + \ln p(C_k)$.

Problem 3 Implement the learning algorithm for the Perceptron discussed in class (on-line version). You can use your favorite programming language to implement the algorithm.

Download the data (from the class webpage) to be used for training and testing of the perceptron. The folder contains ten training sets and one test set. (The file names for the training sets are: *set1.train*, ..., *set10.train*; the file name for the test set is *set.test*.) Each training set contains 40 two-dimensional points, each associated with the corresponding class label (either 0 or 1). The test set contains 2000 points. Points in the test set are also associated with the corresponding class label (to compute misclassification errors). For all given sets, points of one class are drawn from the same underlying distribution. The structure of each file is as follows:

x_1 y_1 $label_1$
x_2 y_2 $label_2$
...
x_i y_i $label_i$

Use each training set to train the perceptron, then use the test data to compute the misclassification error. Initialize the weights randomly before each training phase. This process will give you ten trained perceptrons and 10 error rates. Plot each training set and corresponding decision boundary. Also plot each learned decision boundary (separately) along with the test set. Use your favorite program to do the scatterplots (e.g., Matlab, Gnuplot, Excel, etc.). For each training set, report the number of times (iterations) you provided the sequence as input to the perceptron during training.

Comment your results. What can we say about the training data sets? Does the solution found by the perceptron change for different training data? How about the misclassification error? Motivate your findings.

Instructions to submit Turn in a hard copy of your solution for **Problem 3** only on October 1 in class. Turn in the source code electronically as an attachment by email to carlotta@cs.gmu.edu. Make sure your code compiles and runs properly.