Example:

Suppose we want to build a classifier that recognizes WebPages of graduate students.

How can we find training data?

We can browse the web and collect a sample of WebPages of graduate students of various universities.

Now we have a collection of *positive examples*.

How about *negative examples* ?

The negative examples are... the rest of the web that is not "a graduate student webpage".

So: the negatives examples come from an unknown number of different "negatives" classes.

Thus: It is hopeless, and wrong, to trying to characterize the distribution of the negatives; they can belong to *any* class. ("Each negative examples is negative in its own way.") We just *cannot* formulate this problem as a two class classification problem. **It can be seen as a** (1+x)-class learning problem: There are an unknown number (x) of classes, but the user is interested in one class, i.e. the user is biased toward one class. Similarly: in *content-based image retrieval*, and *document retrieval* in general.

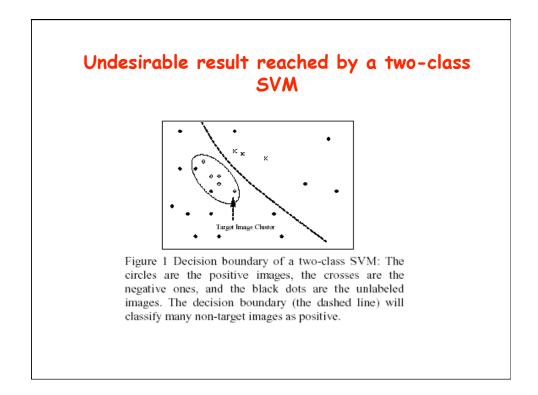
How do we approach this problem then?

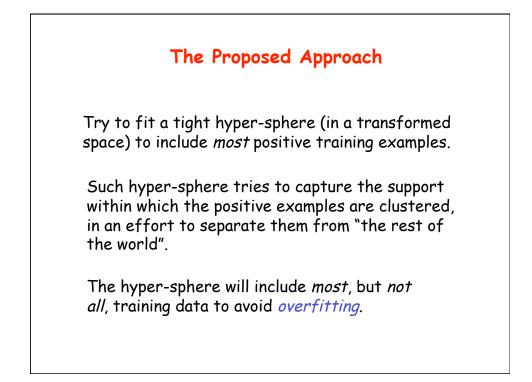
It is reasonable to assume that positive examples cluster in a certain way. ("All positive example are alike.")

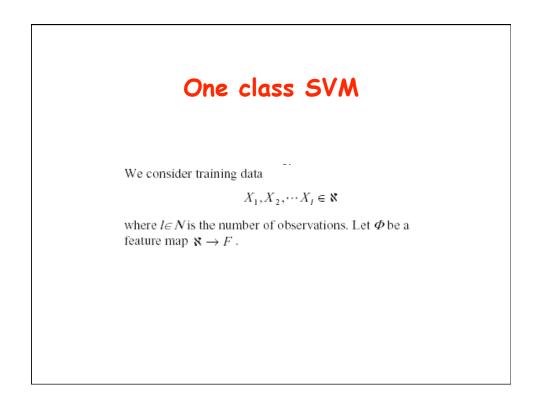
Thus: We can attempt to capture the distribution of the positive examples.

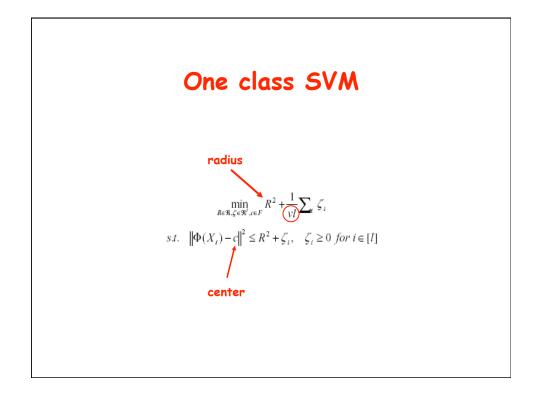
One-class SVMs offer a solution to the (1+x)-class problem.

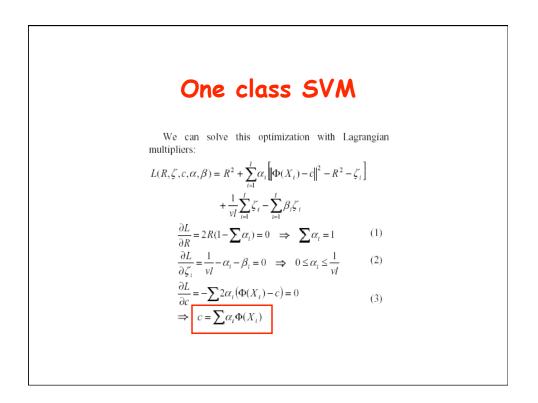








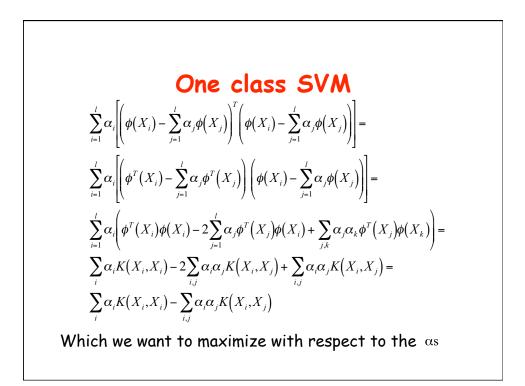


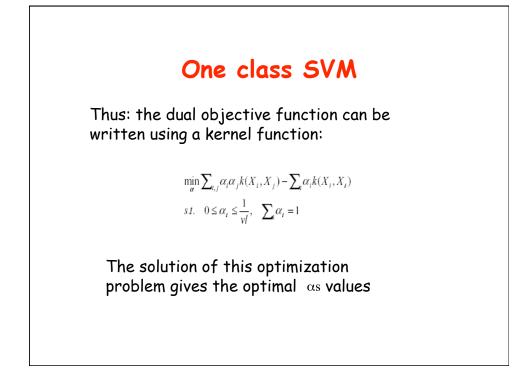


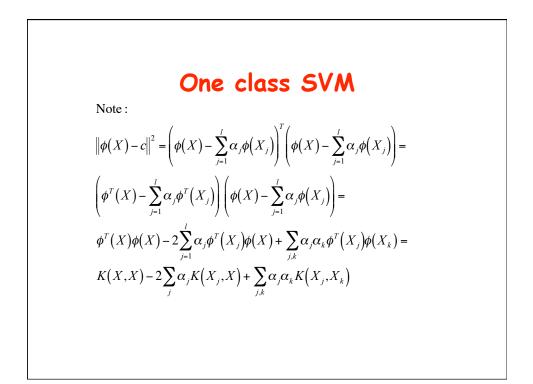
One class SVM

By substituting (1), (2), (3) in L, we obtain:

$$R^{2} + \sum_{i=1}^{l} \alpha_{i} \left[\left(\phi(X_{i}) - \sum_{j=1}^{l} \alpha_{j} \phi(X_{j}) \right)^{T} \left(\phi(X_{i}) - \sum_{j=1}^{l} \alpha_{j} \phi(X_{j}) \right) \right] + \\
-R^{2} - \sum_{i=1}^{l} \alpha_{i} \zeta_{i} + \frac{1}{\nu l} \sum_{i=1}^{l} \zeta_{i} - \sum_{i=1}^{l} \beta_{i} \zeta_{i} = \\
\sum_{i=1}^{l} \alpha_{i} \left[\left(\phi(X_{i}) - \sum_{j=1}^{l} \alpha_{j} \phi(X_{j}) \right)^{T} \left(\phi(X_{i}) - \sum_{j=1}^{l} \alpha_{j} \phi(X_{j}) \right) \right] + \\
+ \sum_{i=1}^{l} \left(\frac{1}{\nu l} - \alpha_{i} - \beta_{i} \right) \zeta_{i} = \sum_{i=1}^{l} \alpha_{i} \left[\left(\phi(X_{i}) - \sum_{j=1}^{l} \alpha_{j} \phi(X_{j}) \right)^{T} \left(\phi(X_{i}) - \sum_{j=1}^{l} \alpha_{j} \phi(X_{j}) \right) \right] +$$







One class SVM

To use the one - class SVM to rank images:

$$f(X) = R^{2} - \left\|\phi(X) - c\right\|^{2} =$$

$$R^{2} - K(X, X) + 2\sum_{j} \alpha_{j} K(X_{j}, X) - \sum_{j,k} \alpha_{j} \alpha_{k} K(X_{j}, X_{k})$$

The closer the image is to the center of the hyper-sphere, the higher is the score, and more likely the image is to be a target image.

