Summer Lecture Series 2002

Introduction to Schema Theory

A survey lecture of pessimistic & exact schema theory

Overview and References

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Overview

One of the earliest attempts to understand how genetic algorithms (GAs) work in a formal sense was through the use of *schema theory*. In schema theory, the search space is partitioned into subspaces of varying levels of generality, and mathematical models are constructed which estimate how the number of individuals in the population belonging to certain schema can be expected to grow in the next generation. From this model arose the *building block hypothesis* (BBH), which attempted to explain how a GA solves a problem by positing that near optimal solutions were forged from small, low-order, fitter-than-average schemata.

Though long-term solutions can be obtained from certain schema theorems, the mathematics for such things often becomes quite difficult without the inclusion of infinite population assumptions and the use of Markov modeling methods. Moreover, the vast majority of schema theoretic results have concentrated on what happens from one generation to the next. For this reason schema theory can be considered a *Local Analysis* method.

Much controversy has surrounded schema theory. The main contention has been its apparent lack of utility. Opponents of schema theory argue that it tells us very little about what is really going on inside an EA. Moreover, the traditional Holland/Goldberg schema theorem is pessimistic in the sense that it provides only a lower bound on expected schema growth. Further, it was traditionally developed for GAs with fixed-length, binary representation using standard GA genetic operators.

However, there has been a recent resurgence of interest in schema theory, brought on in part by researchers such as Riccardo Poli and Bill Langdon. The Poli-Langdon schema theory for genetic programming (GP) opens up new directions in analysis of EAs because it is exact, in the sense that there are tight bounds on the expectation with a known certainty, and also because this new exact schema theory is a generalization of existing schema theory. More importantly, it establishes a framework from which new schema theorems may be constructed, and provides some advice and establishing the appropriate level of granularity of analytical models.

In this lecture, we will review traditional schema theory in the broader context of pessimistic schema theory, then discuss exact schema theoretic models. We will conclude with a short discussion of what schema theory can and cannot do.

- Part I: Overview of Schema Theory
- Part II: Pessimistic Schema Theory
- Part III: Exact Schema Theory
- Part IV: Conclusions

References

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